Fast Density Based Clustering Algorithm

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Abstract—Clustering problem is an unsupervised learning problem. It is a procedure that partition data objects into matching clusters. The data objects in the same cluster are quite similar to each other and dissimilar in the other clusters. The traditional algorithms do not meet the latest multiple requirements simultaneously for objects. Density-based clustering algorithms find clusters based on density of data points in a region. DBSCAN algorithm is one of the density-based clustering algorithms. It can discover clusters with arbitrary shapes and only requires two input parameters. In this paper, we propose a new algorithm based on DBSCAN. We design a new method for automatic parameters generation that create clusters with different densities and generates arbitrary shaped clusters. The k-d tree is used for increasing the memory efficiency. The performance of proposed algorithm is compared with DBSCAN. Experimental results indicate the superiority of proposed algorithm.

Index Terms—Clustering algorithm, k-d-tree, density based algorithm.

I. INTRODUCTION

Clustering is one of the major data mining tasks and aims at grouping the data objects into meaningful classes (clusters) such that the similarity of objects within clusters is maximized, and the similarity of objects from different clusters is minimized [1]. Cluster analysis is one of the main tools for exploring the underlying structure of a data set. Several application domains such as molecular biology, medical applications like breast cancer and geography produce a tremendous amount of data which can no longer be managed without the help of efficient and effective data mining methods. There is an ever increasing need for efficient and effective data mining methods to make use of the information contained implicitly in that data. One of the primary data mining tasks is clustering, which is intended to help a user discovering and understanding the natural structure or grouping in a data set. In particular, clustering is the task of partitioning objects of a data set into distinct groups (clusters) such that two objects from one cluster are similar to each other, whereas two objects from distinct clusters are not. However, traditional clustering algorithms often fail to meet the latest multiple requirements simultaneously. The k-means [1] method is the standard clustering algorithm, enjoys widespread use. The method partitions the data into k clusters, where the k is supplied by the user. DBSCAN (Density Based Spatial Clustering of Applications with Noise) relying on a density-based notion of clusters which is designed to discover clusters of arbitrary shape. DBSCAN [2] requires only one input parameter and supports the user in determining an appropriate value for it. DBSCAN is significantly more effective in discovering clusters of arbitrary shape. DBCLASD [3] is another density-based clustering algorithm, but unlike DBSCAN, the algorithm assumes that the points inside each cluster are uniformly distributed. CLIQUE [4] has been designed to find clusters embedded in subspaces of high dimensional data without requiring the user to guess subspaces that might have interesting clusters. CLIQUE generates cluster descriptions in the form of DNF expressions that are minimized for ease of comprehension. OPTICS is an algorithm for finding density-based clusters in spatial data [5]. Its basic idea is similar to DBSCAN but it addresses one of DBSCAN major weaknesses: the problem of detecting meaningful clusters in data of varying density. In order to do so, the points of the database are (linearly) ordered such that points which are spatially closest become neighbors in the ordering. Additionally, a special distance is stored for each point that represents the density that needs to be accepted for a cluster in order to have both points belong to the same cluster. The DENCLUE algorithm employs a cluster model based on kernel density estimation [6]. A cluster is defined by a local maximum of the estimated density function. Data points are assigned to clusters by hill climbing, i.e. points going to the same local maximum are put into the same cluster. Rough-DBSCAN [8] is a Density based clustering techniques like DBSCAN are attractive because it can find arbitrary shaped clusters along with noisy outliers. MITOSIS [10] finds arbitrary shapes of arbitrary densities in high dimensional data. Unlike previous algorithms, this algorithm uses a dynamic model that combines both local and global distance measures. The algorithm's ability to distinguish arbitrary densities in a complexity of order $O(D_n \log (n))$ renders it attractive to use. Validity indexes indicate that Mitosis out performs related algorithms as DBSCAN [2], which finds clusters of arbitrary shapes. In DENCOS [9] different density thresholds is utilized to discover the clusters in different subspace cardinalities to cope up with density divergence problem. Here the dense unit discovery is performed by utilizing a novel data structure DFP-tree (Density FP-tree), which is constructed on the data set to store the complete information of the dense units. As validated by our extensive experiments on various data sets, DENCOS can discover the clusters in all subspaces with high quality, and the efficiency of DENCOS outperforms previous works. PACA-DBSCAN [11] is based on partitioning-based DBSCAN and modified ant clustering algorithms. It can partition database into N partitions according to the density.
of data, then cluster each partition with DBSCAN [2]. Superior to DBSCAN, The new hybrid algorithm reduces the sensitivity to the initial parameters, and can deal with data of uneven density very well. APSCAN [12] is a parameter free clustering algorithm. The APSCAN has two advantages: first it does not need to predefine the two parameters as required in DBSCAN [2] and second, it not only can cluster datasets with varying densities but also preserve the nonlinear data structure for such datasets.

This paper is organized as follows. Density based definitions are given in Section 2. In Section 3 Proposed Fast Density Based Algorithm is explained. Section 4 contains data description and result analysis. Finally, we conclude in Section 5.

II. DENSITY BASED DEFINITIONS FOR CLUSTERS
Definition 1: (directly density-reachable) A point \( p \) is directly density-reachable from a point \( q \) wrt. \( \varepsilon \), MinPts if
1) \( p \in \varepsilon (q) \) and
2) \( |N \varepsilon (q)| \geq \text{MinPts} \) (core point condition).

Definition 2: (density-reachable) A point \( p \) is density-reachable from a point \( q \) wrt. \( \varepsilon \) and MinPts if there is a chain of points \( p_1, \ldots, p_n = q \), \( p_i = p \) such that \( p_{i+1} \) is directly density-reachable from \( p_i \).

Definition 3: (density-connected) A point \( p \) is density-connected to a point \( q \) wrt. \( \varepsilon \) and MinPts if there is a point \( o \) such that both, \( p \) and \( q \) are density-reachable from \( o \) wrt. \( \varepsilon \) and MinPts.

Definition 4: (cluster) Let \( D \) be a database of points. A cluster \( C \) wrt. \( \varepsilon \) and MinPts is a non-empty subset of \( D \) satisfying the following conditions:
1) If \( p \in C \) and \( q \) is density-reachable from \( p \) wrt. \( \varepsilon \) and MinPts, then \( q \in C \). (Maximality).
2) If \( p, q \in C \): \( p \) is density-connected to \( q \) wrt. \( \varepsilon \) and MinPts. (Connectivity)

Definition 5: (noise) Let \( C_1, \ldots, C_k \) be the clusters of the database \( D \) wrt. Parameters \( \varepsilon \) and MinPts, \( i = 1, \ldots, k \). Then we define the noise as the set of points in the database \( D \) not belonging to any cluster \( C_i \), i.e. noise = \{ \( p \in D \mid p \notin C_i \} \).

III. PROPOSED DENSITY BASED CLUSTERING ALGORITHM
A. Clustering Problem
Clustering is a formal study of algorithms and methods for classifying objects without category labels. A cluster is a set of objects that are similar to each-other, and objects from different clusters are not similar. The set of \( n \) objects \( X = \{X_1, X_2, \ldots, X_n \} \) is to be clustered. Each \( X \in \mathbb{R}^p \) is an attribute vector consisting of \( p \) real measurements describing the object. The objects are to be clustered into non overlapping groups \( C = \{C_1, C_2, \ldots, C_k \} \) (C is known as a clustering), where \( k \) is the number of clusters, \( C_1 \cap C_2 \cup \ldots \cup C_k = X \), \( C_i \neq \phi \) and \( C_i \cap C_j = \phi \) for \( i \neq j \).

B. Kd-Tree
Kd-tree is a space-partitioning data structure for organizing points in a \( K \)-dimensional space [7]. A Kd-tree uses only those splitting planes that are perpendicular to one of coordinate axes. In the nearest neighbor problem a set of data points in \( d \)-dimensional space is given. These points are preprocessed into a data structure, so that given any query point \( q \); the nearest or generally \( k \) nearest points of \( p \) to \( q \) can be reported efficiently.

C. Determining the Parameters \( \varepsilon \) and \( \text{MinPts} \)
The dynamic method enables two input modes; the automatically generated parameters vary according to different inputs.

1) The distance between two objects
The distance function \( d(a, b) \) measures the dissimilarity of two objects

\[
d(a,b)=\sqrt[2]{f_{\varepsilon}(|X_a - X_b|)^2 + f_{\varepsilon}(|X_a - X_b|)^2 + \ldots + f_{\varepsilon}(|X_a - X_b|)^2}
\]  

where \( a = (x_{a1}, x_{a2}, \ldots, x_{ap}) \) and \( b = (x_{b1}, x_{b2}, \ldots, x_{bp}) \) are two \( p \)-dimensional objects, and \( \varepsilon \) is a positive integer.

2) Automatic parameters generation dynamic method
The proposed algorithm discovers clusters with different densities, by generating multiple pairs of \( \varepsilon \) and MinPts automatically.

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1. Create a kd-tree for the given data \( x_n, i = 1, \ldots, n \).
2. For \( i = 1 \) to total no. of cells
   Calculate distance between each pair of objects in \( C_i \)
   If cell does not contain any input objects,
     then calculate \( \varepsilon \) and MinPts
   Else
     If user submit \( n \) objects as input then
     Calculate \( \varepsilon \) and MinPts
     End if
     End for
3. Update \( \varepsilon \) and MinPts
4. For \( i = 1 \) to NP
   Generate clusters and calculate priority of Each pair
   End for
5. For \( i = 1 \) to NP
   Call DBSCAN (\( \varepsilon \), MinPts, set of objects)
   End for
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Fig. 1. (a) FDBA algorithm.

3) FDBA algorithm

IV. EXPERIMENTAL RESULTS
We tested proposed Fast Density Based Algorithm (FDBA) using several synthetic data sets and real data sets. All experiments were run on a PC with a 2.0GHz processor and 1GB RAM. The synthetic data sets are generated by using the data generation method. The synthetic data sets dimensionalities increased from 2 to 20 and size increased from 250 to 5000. Five real data sets from UCI machine learning repository are also utilized to evaluate the clustering
result of FDBA. These real data sets are the adult data, Iris data, breast cancer, Pima data and the thyroid disease data.

The clustering results of DBSCAN and FDBA algorithm is shown in Fig. 2 and Fig. 3 for synthetic data set. This is a 5-dimensional data set consists of three clusters of 300 data points.

V. CONCLUSION

In this paper we present a new algorithm FDBA based on DBSCAN with a new method for automatic parameters generation. We employ artificial data sets and real data sets to prove the performance of our new proposed algorithm. The results of proposed FDBA are evaluated and compared. The experiment has proved that the performance of proposed algorithm is better than DBSCAN.

REFERENCES


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